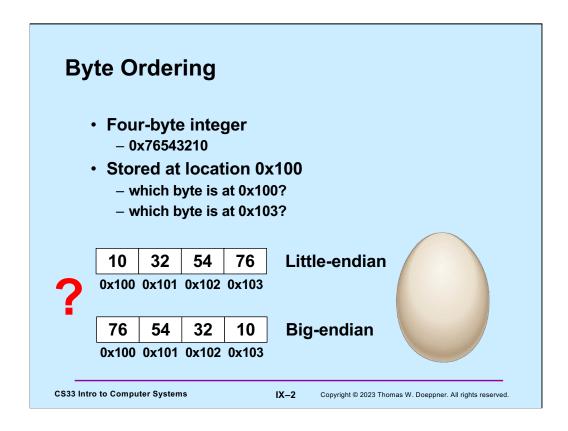


Many of the slides in this lecture are either from or adapted from slides provided by the authors of the textbook "Computer Systems: A Programmer's Perspective." 2^{nd} Edition and are provided from the website of Carnegie-Mellon University, course 15-213, taught by Randy Bryant and David O'Hallaron in Fall 2010. These slides are indicated "Supplied by CMU" in the notes section of the slides.



Read "Gulliver's Travels" by Jonathan Swift for an explanation of the egg.

This code prints out the value of x, one byte at a time, starting with the byte at the lowest address (little end). On x86-based and m1-based (and presumably m2-based) computers, it will print:

00010203

which means that the address of an int is the address of the byte containing its least significant digits (little endian).

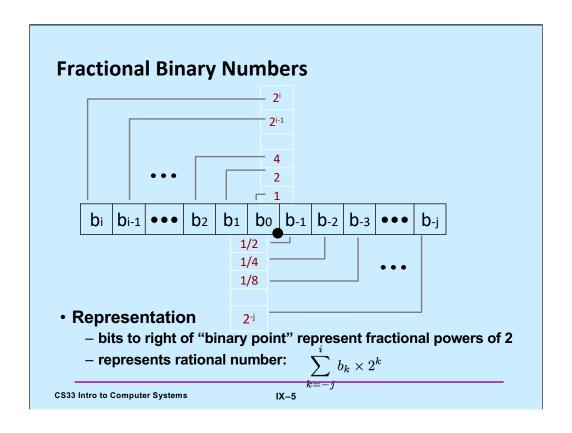
How does **printf** know that **xarray[i]** is an **unsigned char** (and thus one byte long) rather than an **int**? It turns out that **printf** is actually a macro (created using **#define**) that creates additional arguments that give the size (using **sizeof**) of its second and subsequent arguments. Thus, in this example, **printf** calls another function, passing it "%02x", **xarray[i]**, and **sizeof(xarray[i])**. The "%02x" format code says to convert the argument to hexadecimal notation, print it in a field that's two characters wide, and include leading 0s.

Fractional binary numbers • What is 1011.101₂?

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Representable Numbers

- Limitation #1
 - can exactly represent only numbers of the form n/2k
 - » other rational numbers have repeating bit representations
 - value representation
 - » 1/3 0.01010101[01]...2
 - » 1/5 0.001100110011[0011]...2
 - » 1/10 0.0001100110011[0011]...2
- Limitation #2
 - just one setting of decimal point within the w bits
 - » limited range of numbers (very small values? very large?)

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IEEE Floating Point

- IEEE Standard 754
 - established in 1985 as uniform standard for floating point arithmetic
 - » before that, many idiosyncratic formats
 - supported on all major CPUs
- Driven by numerical concerns
 - nice standards for rounding, overflow, underflow
 - hard to make fast in hardware
 - » numerical analysts predominated over hardware designers in defining standard

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IEEE is the Institute for Electrical and Electronics Engineers (pronounced "eye triple e").

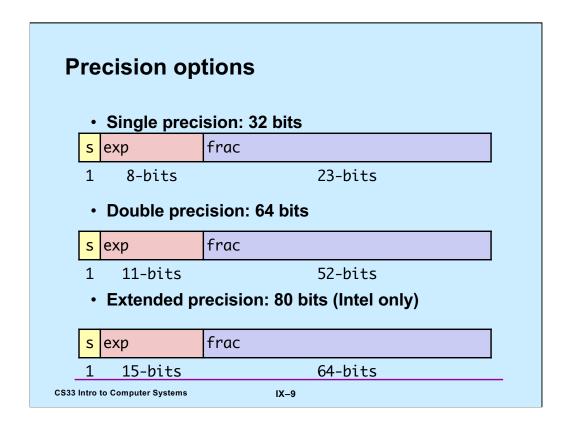
Floating-Point Representation

Numerical Form:

$$(-1)^{s}$$
 M 2^{E}

- sign bit s determines whether number is negative or positive
- significand M normally a fractional value in range [1.0,2.0)
- exponent **E** weights value by power of two
- Encoding
 - MSB s is sign bit s
 - exp field encodes E (but is not equal to E)
 - frac field encodes M (but is not equal to M)

	S	ехр	frac	
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On x86 hardware, all floating-point arithmetic is done with 80 bits, then reduced to either 32 or 64 as required.

"Normalized" Values

- When: exp ≠ 000...0 and exp ≠ 111...1
- Exponent coded as biased value: E = Exp Bias
 - exp: unsigned value exp
 - bias = 2^{k-1} 1, where k is number of exponent bits
 - » single precision: 127 (Exp: 1...254, E: -126...127)
 - » double precision: 1023 (Exp: 1...2046, E: -1022...1023)
- Significand coded with implied leading 1: M = 1.xxx...x2
 - xxx...x: bits of frac
 - minimum when frac=000...0 (M = 1.0)
 - maximum when frac=111...1 (M = 2.0ϵ)
 - get extra leading bit for "free"

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Normalized Encoding Example • Value: float F = 15213.0; $-15213_{10} = 11101101101101_2$ = $1.1101101101101_2 \times 2^{13}$ Significand $M = 1.\underline{1101101101101}_2$ 1101101101101000000000002 frac = Exponent E = 13 bias = 127 exp = **140** = 10001100₂ Result: exp frac IX-11 CS33 Intro to Computer Systems

Denormalized Values

- Condition: exp = 000...0
- Exponent value: E = -Bias + 1 (instead of E = 0 Bias)
- Significand coded with implied leading 0:

 $M = 0.xxx...x_2$

- xxx...x: bits of frac
- Cases
 - $\exp = 000...0$, frac = 000...0
 - » represents zero value
 - » note distinct values: +0 and -0 (why?)
 - $-\exp = 000...0$, frac $\neq 000...0$
 - » numbers closest to 0.0
 - » equispaced

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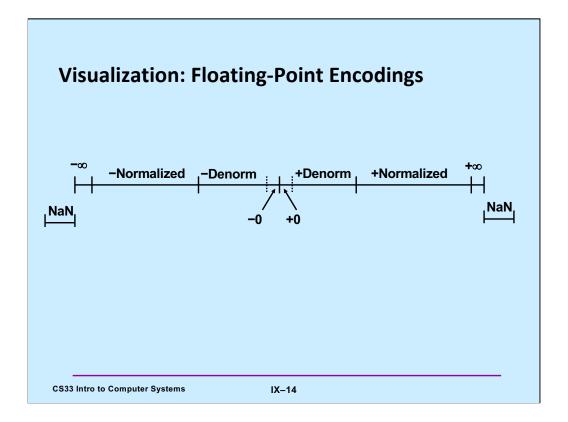
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Special Values

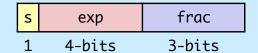
- Condition: exp = 111...1
- Case: exp = 111...1, frac = 000...0
 - represents value ∞ (infinity)
 - operation that overflows
 - both positive and negative
 - $e.g., 1.0/0.0 = -1.0/-0.0 = +\infty, 1.0/-0.0 = -\infty$
- Case: exp = 111...1, $frac \neq 000...0$
 - not-a-number (NaN)
 - represents case when no numeric value can be determined
 - e.g., sqrt(-1), ∞ ∞ , ∞ × 0

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Tiny Floating-Point Example

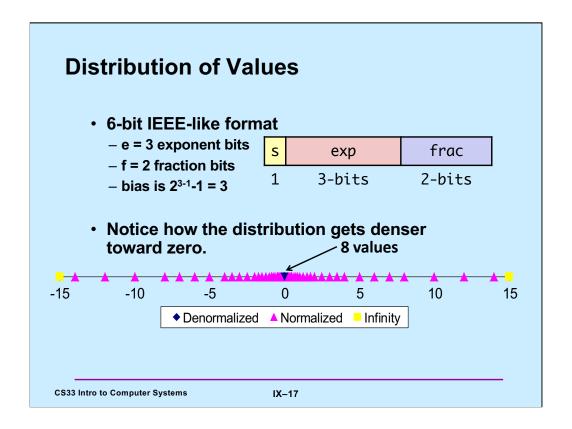


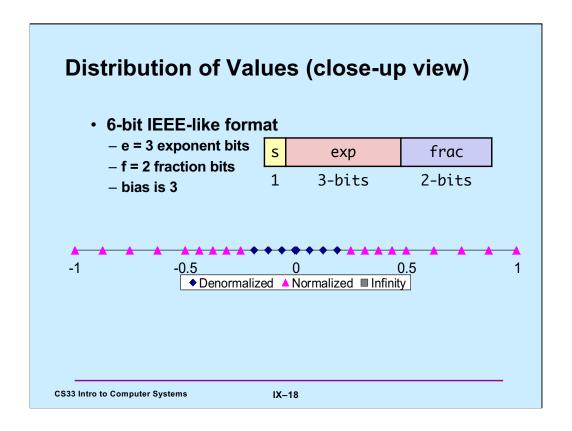
- 8-bit Floating Point Representation
 - the sign bit is in the most significant bit
 - the next four bits are the exponent, with a bias of 7
 - the last three bits are the frac
- Same general form as IEEE Format
 - normalized, denormalized
 - representation of 0, NaN, infinity

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Dynamic Range (Positive Only)							
	s exp frac	E	Value				
	0 0000 000	-6	0				
	0 0000 001	-6	1/8*1/64 = 1/512	closest to zero			
Denormalized numbers	0 0000 010	-6	2/8*1/64 = 2/512	0103031 10 2010			
	0 0000 110	-6	6/8*1/64 = 6/512				
	0 0000 111	-6	7/8*1/64 = 7/512	largest denorm			
	0 0001 000	-6	8/8*1/64 = 8/512	smallest norm			
	0 0001 001	-6	9/8*1/64 = 9/512				
	0 0110 110	-1	14/8*1/2 = 14/16				
	0 0110 111	-1	15/8*1/2 = 15/16	closest to 1 below			
Normalized	0 0111 000	0	8/8*1 = 1				
numbers	0 0111 001	0	9/8*1 = 9/8	closest to 1 above			
	0 0111 010	0	10/8*1 = 10/8				
	0 1110 110	7	14/8*128 = 224				
	0 1110 111	7	15/8*128 = 240	largest norm			
	0 1111 000	n/a	inf	J			
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Quiz 1

- 6-bit IEEE-like format
 - e = 3 exponent bits
 - f = 2 fraction bits
 - bias is 3

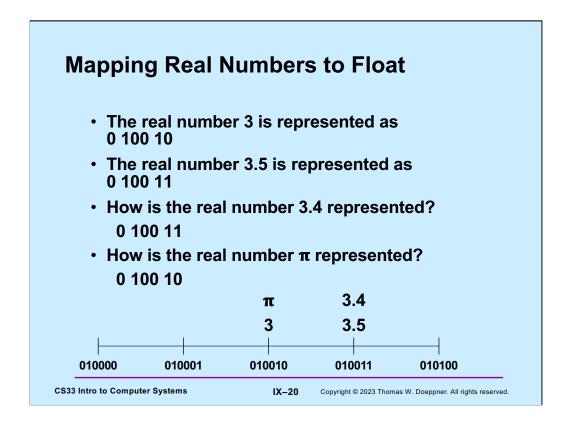
S	exp	frac
1	3-bits	2-bits

What number is represented by 0 010 10?

- a) 3
- b) 1.5
- c) .75
- d) none of the above

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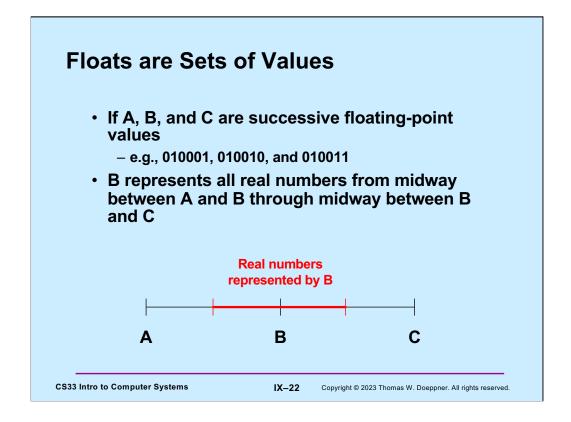
We're assuming here the six-bit floating-point format.

Mapping Real Numbers to Float

- If R is a real number, it's mapped to the floating-point number whose value is closest to R
- · What if it's midway between two values?
 - rounding rules determine outcome

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A special case is 0. Positive 0 represents a range of values that are greater than or equal to 0. Negative 0 represents a range of values that are less than or equal to zero.

Significance

- Normalized numbers
 - for a particular exponent value E and an S-bit significand, the range from 2^E up to 2^{E+1} is divided into 2^S equi-spaced floating-point values
 - » thus each floating-point value represents 1/2^s of the range of values with that exponent
 - » all bits of the significand are important
 - » we say that there are S significant bits for reasonably large S, each floating-point value covers a rather small part of the range
 - · high accuracy
 - for S=23 (32-bit float), accurate to one in 2²³ (.0000119% accuracy)

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Significance

- Unnormalized numbers
 - high-order zero bits of the significand aren't important
 - in 8-bit floating point, 0 0000 001 represents 2-9
 - » it is the only value with that exponent: 1 significant bit (either 2⁻⁹ or 0)
 - » 50% accuracy
 - 0 0000 010 represents 2-8
 0 0000 011 represents 1.5*2-8
 - » only two values with exponent -8: 2 significant bits (encoding those two values, as well as 2-9 and 0)
 - » 25% accuracy
 - fewer significant bits means less accuracy
 - 0 0000 001 represents a range of values from .5*2-9 to 1.5*2-9

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Recall that the bias for the exponent of 8-bit IEEE FP is 7, thus for unnormalized numbers the actual exponent is -6 (-bias+1). The significand has an implied leading 0, thus $0\,0000\,001$ represents $2^{-6} * 2^{-3}$.

With 8-bit IEEE FP. the value 0 0000 01 is interpreted as 2⁻⁹, but the number represented could be 50% less or 50% more.

+/- Zero

- Only one zero for ints
 - an int is a single number, not a range of numbers, thus there can be only zero
- Floating-point zero
 - a range of numbers around the real 0
 - it really matters which side of 0 we're on!
 - » a very large negative number divided by a very small negative number should be positive

$$-\infty/-0 = +\infty$$

» a very large positive number divided by a very small negative number should be negative

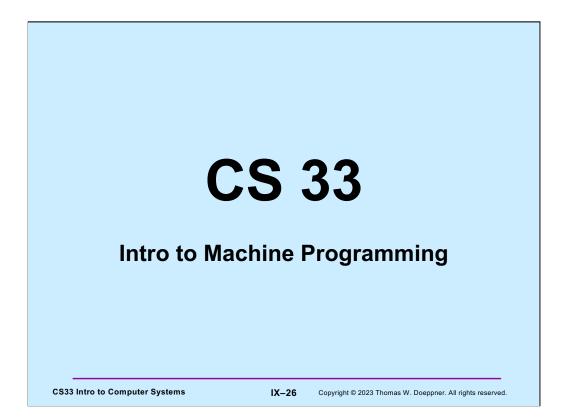
$$+\infty/-0=-\infty$$

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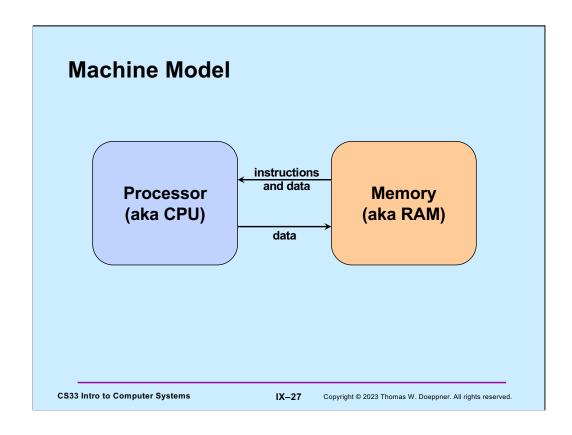
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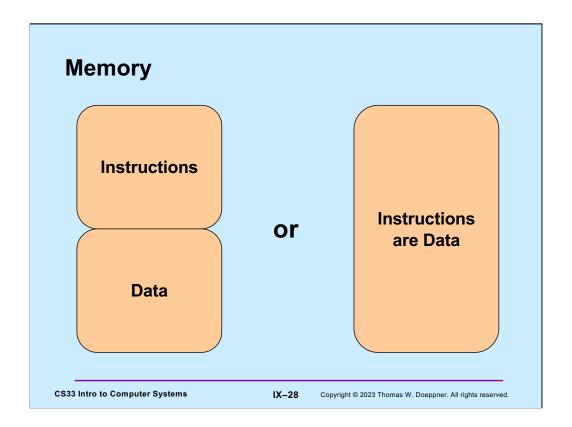
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It's important to remember that a floating-point value is not a single number, but a range of numbers.



We begin our discussion of machine programming by covering some of the general principles involved. We look at a generic "machine language" that is similar, but not identical, to that used on Intel processors. After this brief introduction, we focus on the machine language used by Intel processors.





Generally, we think of their being two sorts of memory: that containing instructions and that containing data. Programs, in general, don't modify their own instructions on the fly. In reality, there's only one sort of memory, which holds everything. However, we arrange so that memory holding instructions cannot be modified and that, usually, memory holding data cannot be executed as instructions.

Of course, programs such as compilers and linkers produce executable code as data, but they don't directly execute it.

Processor: Some Details

Execution engine

Instruction pointer

Condition codes

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Processor: Basic Operation

```
while (forever) {
  fetch instruction IP points at
  decode instruction
  fetch operands
  execute
  store results
  update IP and condition code
}
```

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Instructions ...

Op code | Operand1 | Operand2 | ...

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Operands

- Form
 - immediate vs. reference
 - » value vs. address
- How many?
 - 3

 » add a,b,c

 c = a + b

 2

 » add a,b

 b += a

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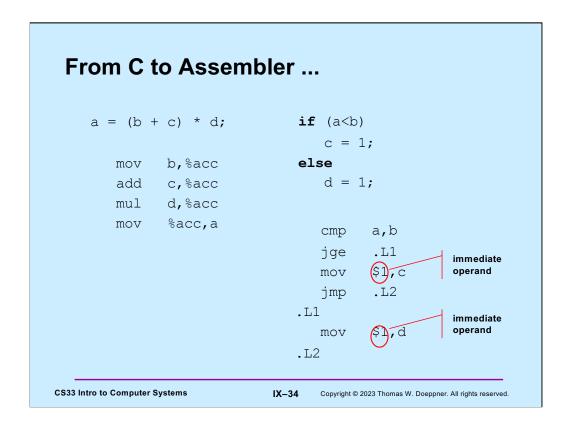
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Operands (continued)

- Accumulator
 - special memory in the processor
 - » known as a register
 - » fast access
 - allows single-operand instructions
 - » add a
 - acc += a
 - » add b
 - acc += b

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Note we're using the accumulator in two-operand instructions. The "%" makes it clear that "acc" is a register. The "\$" indicates that what follows is an immediate operand; i.e., it's a value to be used as is, rather than as an address or a register.

Condition Codes

- Set of flags giving status of most recent operation:
 - zero flag
 - » result was zero
 - sign flag
 - » for signed arithmetic interpretation: sign bit is set
 - overflow flag
 - » for signed arithmetic interpretation
 - carry flag (generated by carry or borrow out of mostsignificant bit)
 - » for unsigned arithmetic interpretation
- Set implicitly by arithmetic instructions
- Set explicitly by compare instruction
 - cmp a,b
 - » sets flags based on result of b-a

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We have one set of arithmetic instructions that work with both unsigned and signed (two's complement) interpretations of the bit values in a word.

The overflow flag is set when the result, interpreted as a two's-complement value should be positive, but won't fit in the word and thus becomes a negative number, or should be negative, but won't fit in the word and thus becomes a positive number.

The carry flag is set when computing the result, interpreted as an unsigned value, requires a borrow out of the most-significant bit (i.e., computing b-a when a is greater than b), or when it results in an overflow (e.g., for 32-bit unsigned integers, when the result should be greater than or equal to 2^{32} (but can't fit in a 32-bit word).

Examples (1)

- Assume 32-bit arithmetic
- x is 0x80000000
 - TMIN if interpreted as two's-complement
 - 231 if interpreted as unsigned
- x-1 (0x7ffffffff)
 - TMAX if interpreted as two's-complement
 - 2³¹-1 if interpreted as unsigned
 - zero flag is not set
 - sign flag is not set
 - overflow flag is set
 - carry flag is not set

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Examples (2)

- x is 0xffffffff
 - -1 if interpreted as two's-complement
 - UMAX (232-1) if interpreted as unsigned
- x+1 (0x00000000)
 - zero under either interpretation
 - zero flag is set
 - sign flag is not set
 - overflow flag is not set
 - carry flag is set

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Examples (3)

- x is 0xffffffff
 - -1 if interpreted as two's-complement
 - UMAX (232-1) if interpreted as unsigned
- x+2 (0x00000001)
 - (+)1 under either interpretation
 - zero flag is not set
 - sign flag is not set
 - overflow flag is not set
 - carry flag is set

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Quiz 2

- Set of flags giving status of most recent operation:
 - zero flag
 - » result was zero
 - sign flag
 - » for signed arithmetic interpretation: sign bit is set
 - overflow flag
 - » for signed arithmetic interpretation
 - carry flag (generated by carry or borrow out of most-significant bit)
 - » for unsigned arithmetic interpretation
- Set explicitly by compare instruction
 - cmp a,b
 - » sets flags based on result of b-a

Which flags are set to one by "cmp \$2,\$1"?

- a) overflow flag only
- b) carry flag only
- c) sign and carry flags only
- d) sign and overflow flags only
- e) sign, overflow, and carry flags

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Jump Instructions

- Unconditional jump
 - just do it
- Conditional jump
 - to jump or not to jump determined by conditioncode flags
 - field in the op code indicates how this is computed
 - in assembler language, simply say
 - » je
 - · jump on equal
 - » jne
 - jump on not equal
 - » jg
 - jump on greater than (signed)
 - » etc.

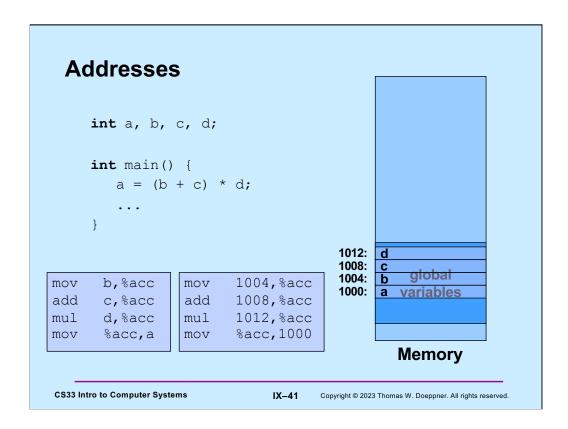
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Jump instructions cause the processor to start executing instructions at some specified address. For conditional jump instructions, whether to jump or not is determined by the values of the condition codes. Fortunately, rather than having to specify explicitly those values, one may use mnemonics as shown in the slide.

We'll see examples of their use in an upcoming lecture, when we're looking at x86 assembler instructions.

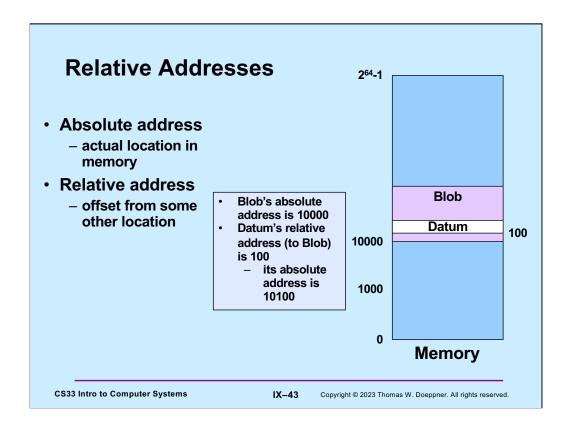


In the C code above, the assignment to a might be coded in assembler as shown in the box in the lower left. But this brings up the question, where are the values represented by \mathbf{a} , \mathbf{b} , \mathbf{c} , and \mathbf{d} ? Variable names are part of the C language, not assembler. Let's assume that these global variables are located at addresses 1000, 1004, 1008, and 1012, as shown on the right. Thus, correct assembler language would be as in the middle box, which deals with addresses, not variable names. Note that "mov 1004,%acc" means to copy the contents of location 1004 to the accumulator register; it does not mean to copy the integer 1004 into the register!

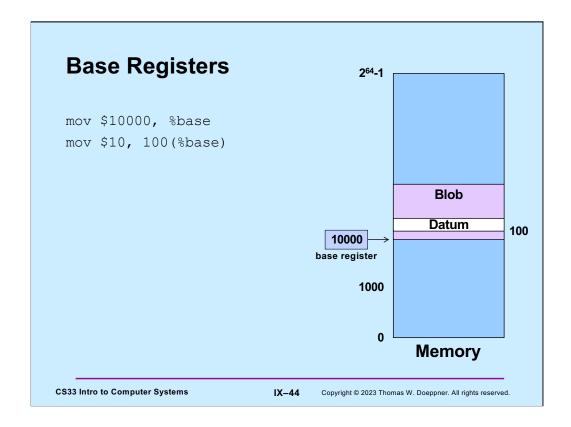
Beginning with this slide, whenever we draw pictures of memory, lower memory addresses are at the bottom, higher addresses are at the top. This is the opposite of how we've been drawing pictures of memory in previous slides.

```
Addresses
     int b;
     int func(int c, int d) {
         int a;
         a = (b + c) * d;
                                 • One copy of b for duration of
                                    program's execution
     }
                                     • b's address is the same
                                         for each call to func
                  ?, %acc
         mov
                                 • Different copies of a, c, and d
                  ?,%acc
         add
                                    for each call to func
                                        addresses are different in
                  ?,%acc
         mul
                                         each call
                  %acc,?
         mov
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                                   IX-42
                                          Copyright © 2023 Thomas W. Doeppner. All rights reserved.
```

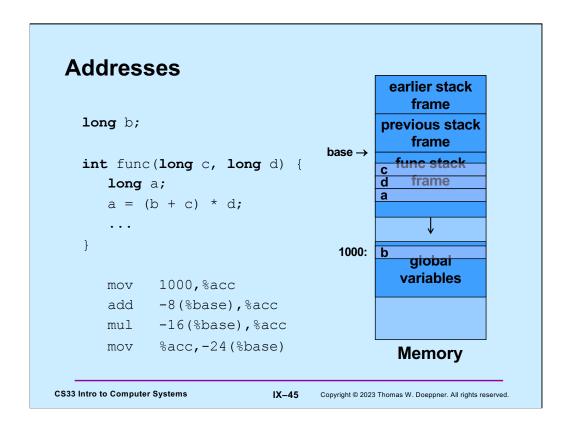
Here we rearrange things a bit. **b** is a global variable, but a is a local variable within **func**, and **c** and **d** are arguments. The issue here is that the locations associated with **a**, **c**, and **d** will, in general, be different for each call to **func**. Thus, we somehow must modify the assembler code to take this into account.



Note that both positive and negative offsets might be used.



Here we load the value 10,000 into the base register (recall that the "\$" means what follows is a literal value; a "%" sign means that what follows is the name of a register), then store the value 10 into the memory location 10100 (the contents of the base register plus 100): the notation \mathbf{n} (%base) means the address obtained by adding \mathbf{n} to the contents of the base register.



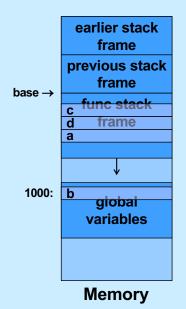
Here we return to our earlier example. We assume that, as part of the call to **func**, the base register is loaded with the address of the beginning of **func**'s current stack frame, and that the local variable **a** and the parameters **c** and **d** are located within the frame. Thus, we refer to them by their offset from the beginning of the stack frame, which are assumed to be **-24**, **-8**, and **-16**. Since the stack grows from higher addresses to lower addresses, these offsets are negative. Note that the first assembler instruction copies the contents of location 1000 into **%acc**.

Quiz 3

Suppose the value in *base* is 10,000. What is the address of *c*?

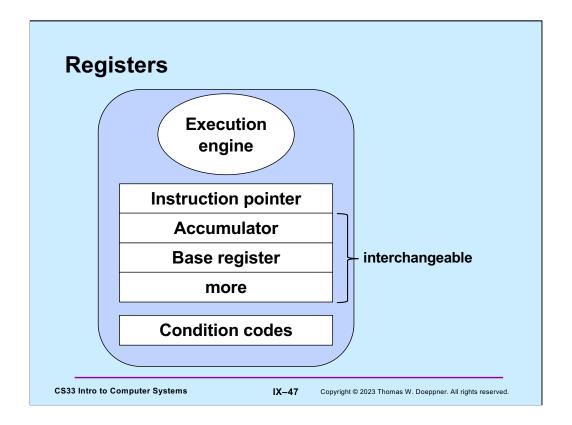
- a) 10,016
- b) 10,008
- c) 9992
- d) 9984

```
mov 1000, %acc
add -8 (%base), %acc
mul -12 (%base), %acc
mov %acc, -16 (%base)
```

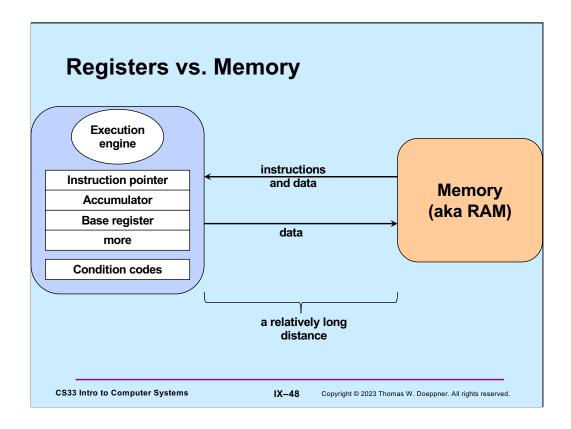


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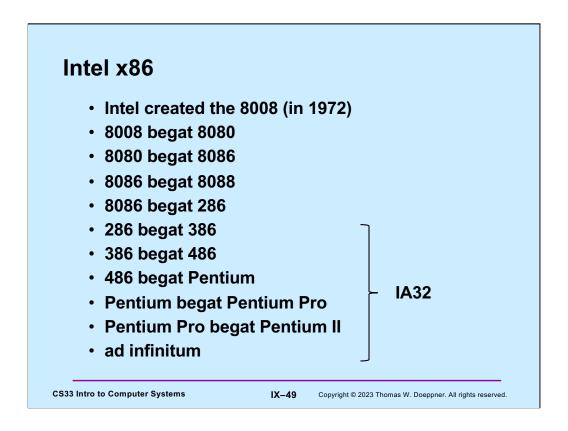


We've now seen four registers: the instruction pointer, the accumulator, the base register, and the condition codes. The accumulator is used to hold intermediate results for arithmetic; the base register is used to hold addresses for relative addressing. There's no particular reason why the accumulator can't be used as the base register and vice versa: thus, they may be used interchangeably. Furthermore, it is useful to have more than two such dual-purpose registers. As we will see, the x86 architecture has eight such registers; the x86-64 architecture has 16.



Why do we make the distinction between registers and memory? Registers are in the processor itself and can be read from and written to very quickly. Memory is on separate hardware and takes much more time to access than registers do. Thus, operations involving only registers can be executed very quickly, while significantly more time is required to access memory. Processors typically have relatively few registers (the IA-32 architecture has eight, the x86-64 architecture has 16; some other architectures have many more, perhaps as many as 256); memory is measured in gigabytes.

Note that memory access-time is mitigated by the use of in-processor caches, something that we will discuss in a few weeks.



The early computers of the x86 family had 16-bit words; starting with the 386, they supported 32-bit words.

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- 2³² used to be considered a large number
 - one couldn't afford 2³² bytes of memory, so no problem with that as an upper bound
- Intel (and others) saw need for machines with 64-bit addresses
 - devised IA64 architecture with HP
 - » became known as Itanium
 - » very different from x86
- AMD also saw such a need
 - developed 64-bit extension to x86, called x86-64
- Itanium flopped
- x86-64 dominated
- Intel, reluctantly, adopted x86-64

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 2^{32} = 4 gigabytes.

 2^{64} = 16 exbibytes.

All SunLab computers are x86-64.

Why Intel?

- Most CS Department machines are Intel
- An increasing number of personal machines are not
 - Apple has switched to ARM
 - packaged into their M1, M2, etc. chips"Apple Silicon"
- Intel x86-64 is very different from ARM64 internally
- Programming concepts are similar
- We cover Intel; most of the concepts apply to ARM

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ARM originally stood for Acorn RISC machine. Acorn was a British computer company that was established in 1978, but no longer exists. RISC stands for Reduced Instruction Set Computer. The RISC concept was devised in the 1980s and was very popular in the 80s and 90s. The idea is to design computers with relatively few instructions, but implement those instructions so they can execute very quickly. The fastest computers in the 80s and 90s were RISC computers. But Intel, who built computer chips with fairly complex instruction sets (CISC), learned how to make their computers run really fast as well. That, coupled with the fact that Windows ran exclusively on Intel, helped Intel stay in the lead.

ARM later became Advanced RISC Machine. Now, it doesn't stand for anything, It's just ARM.

Apple (whose computers originally ran Motorola 68000 processors before they switched to Intel) decided that they could make more cost-effective and faster processors by adapting the ARM design and including GPUs (graphics processing units). GPUs are specialized processors that help with image processing, but also can be used with other computations that have a lot of inherent parallelism. Apple refers to their new chips as M1 and M2 (presumably an M3 is not far behind).